# Extra Time Like Dimensions, Superluminal Motion, and Dark Matter 

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#### Abstract

We show that the superluminal speeds of the muon neutrinos observed in the OPERA experiment can be explained within a relativity theory with extra time like dimensions. In addition, such theory predicts, the existence of dark matter.


## 1 Introduction

The recent OPERA finding of faster-than-light muon neutrinos [1], if confirmed, and if it cannot be explained within the usual physics, will require a reformulation or a generalization of the theory of relativity. There already exist several theories that allow for superluminal motion, and they all contain the Einstein's special relativity as a limiting case, for instance:
I. The extended special relativity with superluminal transformations [2, 3, 4]. The latter theory joins the Bilaniuk-Despande-Sudarshan proposal of tachyons [5] with the principle of relativity.
II. Higher dimensional spaces, $M_{p, q}$, with extra time like and space like dimensions (signature $(p, q)$ ) [6, 7]. In a subspace with signature $(1,3)$ (the Minkowski spacetime $M_{1,3}$ ), particles can move faster than light, if their worldlines are suitably inclined into the extra time like dimensions 8. A candidate for such higher dimensional space is the Clifford space $C_{8,8}$, a manifold whose tangent space at every point is a Clifford algebra $C l(1,3)$, generated by basis vectors of $M_{1,3}$. In the past years an extended relativity theory in Clifford spaces was developed [9]-[12]. As discussed in [11, 9], one can have tachyonic (faster-than-light) behavior in ordinary spacetime, $M_{1,3}$, while having non-tachyonic behavior in $C_{8,8}$.

Besides that, the Stueckelberg theory with an invariant evolution parameter [13, [10], and the relativity in phase space [14] also predict superluminal motions.

In this Letter I will show that the extended special relativity (Case I) cannot explain the OPERA result $v / c-1=2.48 \times 10^{-5}$, because this would require too high neutrino mass. On the other hand, in the presence of extra time like dimensions (Case II), a particle's speed, as observed in the ordinary spacetime, can be greater
than the speed of light, regardless of how small the particle's mass is. Usually, such a possibility of superluminal motion has been considered as an argument against extra time like dimensions. But this argument will no longer hold, if the OPERA result is confirmed.

Moreover, in a space $M_{p, q}$ there exist particle's worldlines that are invisible to certain classes of observers [15, 8]. And vice versa, for a given observer $\mathcal{O}$ in $M_{p, q}$, associated with a worldline $A$, there exist a class of worldlines $\{B\}$ that are invisible to $\mathcal{O}$, because the light cones originating from the points on $B$ do not intersect the observer's worldline $A$. This could be an explanation for dark matter. But such matter would not be really dark, but only invisible to us.

## 2 Faster-than-light motion

### 2.1 Tachyons in the extended special relativity

The possibility of tachyons was proposed by Bilaniuk et al. [5. In 70's the idea attracted considerable attention and the principle of relativity was extended to superluminal transformations [2, 3, 3].

A tachyons's energy is given by

$$
\begin{equation*}
E=\frac{m c^{2}}{\sqrt{\frac{v^{2}}{c^{2}}-1}} \tag{1}
\end{equation*}
$$

From this we find

$$
\begin{equation*}
\frac{v}{c}=\sqrt{1+\frac{m^{2} c^{4}}{E^{2}}} \approx 1+\frac{1}{2} \frac{m^{2} c^{4}}{E^{2}} \tag{2}
\end{equation*}
$$

Taking the OPERA result $v / c-1=2.48 \times 10^{-5}$ and $E=17 \mathrm{GeV}$, we have

$$
\begin{equation*}
m c^{2} \approx E \sqrt{2\left(\frac{v}{c}-1\right)}=17 \times 10^{9} \mathrm{eV} \sqrt{2 \times 2.48 \times 10^{-5}}=120 \mathrm{MeV} \tag{3}
\end{equation*}
$$

Since the muon neutrino mass is much lower, it means that the faster-than-light neutrinos found in the OPERA experiment, cannot be the tachyons of the kind considered in [2]-[5].

On the other hand, the SN1987a neutrinos [16] had energy around 20 MeV and the velocity $v / c-1 \approx 2 \times 10^{-9}$. From Eq. (3) we then obtain $m c^{2} \approx 9 \times 10^{2} \mathrm{eV}$. This also is too high value for the neutrino mass.

### 2.2 Beyond the speed of light in spaces with extra time like dimensions

The idea that spacetime has equal number of space like and time like dimensions has been much explored in the past decades [6, 7]. Let $M_{n, n}$ be a manifold whose points
are described by coordinates $x^{a}=\left(t^{i}, x^{i}\right), i=1,2, \ldots, n$, and the quadratic form is given by

$$
\begin{equation*}
\mathrm{d} s^{2}=\eta_{a b} \mathrm{~d} x^{a} \mathrm{~d} x^{b}=\mathrm{d} t^{i} \mathrm{~d} t_{i}+\mathrm{d} x^{i} \mathrm{~d} x_{i} \tag{4}
\end{equation*}
$$

with the metric $\eta_{a b}=\operatorname{diag}(1,1, \ldots,-1,-1, \ldots)$. We use the units in which the speed of light, defined according to $c^{2}=\left(-\mathrm{d} x^{i} \mathrm{~d} x_{i}\right) /\left(\mathrm{d} t^{i} \mathrm{~d} t_{i}\right)$, is $c=1$.

In such spacetime, the transformations that change the sign of $\mathrm{d} s^{2}$ (the so called 'superluminal transformations' that transform a bradyon into a tachyon), are real. However, a slower than light particle, a bradyon, cannot be accelerated beyond the speed of light and become a tachyon, because of the infinite energy barrier on the light cone in $M_{n, n}$. And yet, if our physical space is of the type $M_{n, n}$, then faster than light travel is possible in principle, because in the 4D subspace $M_{1,3}$, an accelerating particle can become faster than light, without crossing the infinite energy barrier. A particle does not need to cross the light cone in $M_{n, n}$ in order to become superluminal in $M_{1,3}$. Such a particle is not a tachyon in $M_{n, n}$, because its worldline is still subluminal with respect to the light cone in $M_{n, n}$, and the $\mathrm{d} s^{2}$ along the worldline did not change sign.

The action for a massive particle moving in $M_{n, n}$ is

$$
\begin{equation*}
I\left[x^{a}\right]=M \int \mathrm{~d} \tau\left(\dot{x}^{a} \dot{x}^{b} \eta_{a b}\right)^{1 / 2} \tag{5}
\end{equation*}
$$

where $\dot{x}^{a} \equiv \dot{x}^{a}(\tau)$ are functions of an arbitrary parameter $\tau$.
The momentum is

$$
\begin{equation*}
p^{a}=\frac{M \dot{x}^{a}}{\left(\dot{x}^{c} \dot{x}^{d} \eta_{c d}\right)^{1 / 2}}=\left(\tilde{p}^{i}, p^{i}\right) \tag{6}
\end{equation*}
$$

and satisfies the constraint

$$
\begin{equation*}
p^{a} p^{b} \eta_{a b}=M^{2} \tag{7}
\end{equation*}
$$

From now on, we take $n=3$.
Since $\tau$ is arbitrary, we may take $\tau=t^{1}$. Then we have

$$
\begin{equation*}
p^{a}=\frac{M \dot{x}^{a}}{\left(1+\left(\dot{t}^{2}\right)^{2}+\left(\dot{t}^{3}\right)^{2}-(\dot{x})^{1}-(\dot{x})^{2}-(\dot{x})^{3}\right)^{1 / 2}}, \tag{8}
\end{equation*}
$$

where

$$
\begin{equation*}
v^{2} \equiv\left(\dot{x}^{1}\right)^{2}+\left(\dot{x}^{2}\right)^{2}+\left(\dot{x}^{3}\right)^{2}<1+\left(\dot{t}^{2}\right)^{2}+\left(\dot{t}^{3}\right)^{2} \tag{9}
\end{equation*}
$$

and $\dot{x}^{a}=\mathrm{d} x^{a} / \mathrm{d} t^{1}$. From the latter equation it follows that the spatial speed, $v$, can exceed the speed of light, $c=1$, if $w^{2} \equiv\left(\dot{t}^{2}\right)^{2}+\left(\dot{t}^{3}\right)^{2}>0$, while still satisfying the condition $1-v^{1}+w^{2}>0$.

We define the first component as energy ${ }^{1}$

$$
\begin{equation*}
\tilde{p}^{1} \equiv E=\frac{M}{\left(1-v^{2}+w^{2}\right)^{1 / 2}}, \tag{10}
\end{equation*}
$$

from which it follows

$$
\begin{equation*}
w=\sqrt{v^{2}-1+\frac{M^{2}}{E^{2}}} \tag{11}
\end{equation*}
$$

The muon neutrinos of the OPERA experiment had the average energy $E=17 \mathrm{GeV}$ and the velocity $v=1+2,48 \times 10^{-5}$. Using those data in Eq. (11), we obtain

$$
\begin{equation*}
w \approx \sqrt{2(v-1)}=7,04 \times 10^{-3} \tag{12}
\end{equation*}
$$

to which there corresponds the velocity $2.11 \times 10^{6} \mathrm{~m} / \mathrm{s}$. This is the velocity in the direction of the time like dimensions $t^{2}$ and $t^{3}$ that gives the superluminal velocity $v$ of the muon neutrino.

From Eq. (10) we also have

$$
\begin{equation*}
E^{2}=\frac{M^{2}}{1-v^{2}+w^{2}}=\frac{M^{2}}{1-v^{2}} \frac{1-v^{2}}{1-v^{2}+w^{2}}=\frac{m^{2}}{1-v^{2}}, \tag{13}
\end{equation*}
$$

where

$$
\begin{equation*}
m^{2}=M^{2} \frac{1-v^{2}}{1-v^{2}+w^{2}} \tag{14}
\end{equation*}
$$

is the effective mass in 4D Minkowski space spanned over $\left(t^{1}, x^{1}, x^{2}, x^{3}\right)$. The relation (14) is well-known from Kaluza-Klein theories. It is a consequence of the relations

$$
\begin{equation*}
\dot{x}^{a} \dot{x}^{b} \eta_{a b}=\dot{x}^{\mu} \dot{x}^{\nu} \eta_{\mu \nu}+\dot{x}^{\bar{a}} \dot{x}^{\bar{b}} g_{\bar{a} \bar{b}} \tag{15}
\end{equation*}
$$

and

$$
\begin{equation*}
M^{2}=p^{a} p^{b} \eta_{a b}=p^{\mu} p^{\nu} \eta_{\mu \nu}+p^{\bar{a}} p^{\bar{b}} g_{\bar{a} \bar{b}} \tag{16}
\end{equation*}
$$

where $\dot{x}^{\mu}=\left(\dot{t}^{1}, \dot{x}^{1}, \dot{x}^{2}, \dot{x}^{3}\right) \equiv\left(\dot{x}^{0}, \dot{x}^{i}\right)$ is the 4 -velocity, $p^{\mu}=\left(\tilde{p}^{1}, p^{1}, p^{2}, p^{3}\right) \equiv\left(p^{0}, p^{i}\right)$ the 4-momentum, whereas $\dot{x}^{\bar{a}}=\left(\dot{t}^{2}, \dot{t}^{3}\right)$ and $p^{\bar{a}}=\left(\tilde{p}^{2}, \tilde{p}^{3}\right)$ are extra components of velocity and momentum, respectively. Multiplying Eq. (15) with $M^{2}$, using $M^{2}=p^{a} p^{b} \eta_{a b}$, $m^{2}=p^{\mu} p^{\nu} \eta_{\mu \nu}$, and Eq. (6), and identifying $\dot{x}^{i} \dot{x}_{i}=-v^{2}, \dot{x}^{\bar{a}} \dot{x}_{\bar{a}}=\left(\dot{t}^{2}\right)^{2}+\left(\dot{t}^{3}\right)^{2} \equiv w^{2}$, we obtain Eq. (14). Let us also identify $p^{\bar{a}} p^{\bar{b}} g_{\bar{a} \bar{b}}=\left(\tilde{p}^{2}\right)^{2}+\left(\tilde{p}^{3}\right)^{2} \equiv \tilde{q}^{2}$. Then Eq. (16) can be written as

$$
\begin{equation*}
M^{2}=m^{2}+\tilde{q}^{2} \tag{17}
\end{equation*}
$$

[^0]If $w^{2} \neq 0$, then it can be $v^{2}>1+w^{2}>1$. The 4 D mass squared (14) is then negative, $m^{2}<0$. From Eq. (13) we obtain

$$
\begin{equation*}
v^{2}-1=\frac{-m^{2}}{E^{2}}=\frac{\tilde{q}^{2}-M^{2}}{E^{2}} \tag{18}
\end{equation*}
$$

So we have

$$
\begin{equation*}
\sqrt{-m^{2}}=\sqrt{\tilde{q}^{2}-M^{2}} \approx E \sqrt{2(v-1)}=17 \mathrm{GeV} \sqrt{2.48 \times 10^{-5}}=120 \mathrm{MeV} \tag{19}
\end{equation*}
$$

The same equation has been derived in Ref. [14] by a different procedure, starting from the dispersion relations and the expression for the group velocity. It was also observed that the above mass is close to the muon mass $m_{\mu}=105.7 \mathrm{MeV}$. Whether or not this is a coincidence has to be found out by further investigations.

We see that in this model the quantity $m^{2}=M^{2}-\tilde{q}^{2}$ is the effective 4 D mass squared of the muon neutrino. We envisage that at high energies, in the collision processes producing mesons $\pi^{+}, K^{+}$that subsequently decayed into $\mu^{+}$and $\nu_{\mu}$, the particles acquired not only the ordinary spatial momenta $p^{1}, p^{2}, p^{3}$, but also the extra momenta $\tilde{p}^{2}, \tilde{p}^{3}$, which, according to Eq. (19), contributed to the effective 4D mass of $\nu_{\mu}$. According to this theory, the 4D masses of $\nu_{\mu}, \nu_{\tau}$ and $\nu_{e}$ depend on the conditions of the process in which they are produced. In a decay process of a low energy pion, $\pi^{+} \rightarrow \pi^{0}+\mu^{+}+\nu_{\mu}$, with the pion momentum $p^{a}=\left(\tilde{p}^{1}, 0,0 ; p^{1}, p^{2}, p^{3}\right)$, the outgoing $\mu^{+}$and $\nu_{\mu}$ have low spatial momenta, and also low extra momenta $\tilde{p}^{2}, \tilde{p}^{3}$, and they have thus low 4D masses, $m \approx M$.

Neutrino oscillations give us the information about the differences $m_{\nu_{\mu^{\prime}}}^{2}-m_{\nu_{\tau^{\prime}}}^{2}$, $m_{\nu_{\mu^{\prime}}}^{2}-m_{\nu_{e^{\prime}}}^{2}$, etc., but not about the values $m_{\nu_{\mu^{\prime}}}^{2}=M_{\nu_{\mu^{\prime}}}^{2}-\tilde{q}_{\nu_{\mu^{\prime}}}^{2}, m_{\nu_{\tau^{\prime}}}^{2}=M_{\nu_{\tau^{\prime}}}^{2}-\tilde{q}_{\nu_{\tau^{\prime}}}^{2}$, and $m_{\nu_{e^{\prime}}}^{2}=M_{\nu_{e^{\prime}}}^{2}-\tilde{q}_{\nu_{e^{\prime}}}^{2}$. In the above differences, the extra momenta cancel out, if they are all equal to each other. This is indeed the case, because the 6 -momentum must be conserved when one kind of neutrino oscillates into another one in the absence of any external interactions.

## 3 Invisible particles

In a world with multi-time like dimensions, a luminous body is not visible for all observers [15, 8]. For instance, if an observer worldline $A$ is displaced "sidewise" in multi-time with respect to a body's wordlline $B$ (see Fig. 1), then $B$ can be invisible to $A$, and vice versa. This is so, because the light cones originating $\sqrt[3]{ }$ from $B$ do not

[^1]intersect the worldline $A$. A light cone is given by
\[

$$
\begin{equation*}
\left(t^{i}-t_{B}^{i}\right)^{2}-\left(x^{i}-x_{B}^{i}\right)^{2}=0 . \tag{20}
\end{equation*}
$$

\]

Formally, the worldlines of the observer $A$ and the luminous source $B$ are

$$
\begin{equation*}
t^{i}=t_{A}^{i}(\tau), \quad x^{i}=x_{A}^{i}(\tau) ; \quad t^{i}=t_{B}^{i}\left(\tau_{0}\right), \quad x^{i}=x_{B}^{i}\left(\tau_{0}\right) \tag{21}
\end{equation*}
$$

In particular, let the worldline of $A$ be

$$
\begin{gather*}
A: \quad t^{1}=\tau, \quad t^{2}=t_{A}^{2} \neq 0, \quad t^{3}=0, \quad x^{1}=x_{A}^{1} \neq 0, \quad x^{2}=0, \quad x^{3}=0  \tag{22}\\
B: \quad t^{1}=\tau_{0}, \quad t^{2}=0, \quad t^{3}=0, \quad x^{1}=0, \quad x^{2}=0, \quad x^{3}=0 . \tag{23}
\end{gather*}
$$

We thus have $t_{B}^{1}\left(\tau_{0}\right)=\tau_{0}$, which is the time of emission of light.


Figure 1: The light cones originating from the worldine $B$, traced by a luminous source, never intersect the observer's worldline $A$ that is parallelly displaced with respect to $B$ along the direction of $t^{2}$. Therefore, this source is invisible to the observer.

A light cone, emerging from a point on the worldine $B$ is

$$
\begin{equation*}
\left(t^{1}-\tau_{0}\right)^{2}+\left(t^{2}\right)^{2}+\left(t^{3}\right)^{2}-\left(x^{1}\right)^{2}-\left(x^{2}\right)^{2}-\left(x^{3}\right)^{2}=0 \tag{24}
\end{equation*}
$$

Inserting the values for $t^{i}, x^{i}$ of Eq. (22) into Eq. (24), we obtain

$$
\begin{equation*}
\left(\tau-\tau_{0}\right)^{2}+\left(t_{A}^{2}\right)^{2}-\left(x_{A}^{1}\right)^{2}=0 \tag{25}
\end{equation*}
$$

actually, we are interested in the opposite, namely, when the particle (matter) is not seen by the observer. Therefore, I consider the light cones originating form the particle worldline. The procedure that I then employ is just a straightforward application of analytical geometry.

If $\left(t_{A}^{2}\right)^{2}-\left(x_{A}^{1}\right)^{2}>0$, then the system of equations (22) and (24) has no solution, since by our assumption all coordinates are real. Therefore, the light cone (24) and the worldline $A$ have no common point, i.e., they do not intersect. This is true for any value of the parameter $\tau_{0}$, and hence for any point on the source worldline $B$.

In general, the observer's worldline $A$ need not be parallel to that of the source. Let $A$ be given by

$$
\begin{equation*}
t^{1}=u^{1} \tau, \quad t^{2}=u^{2} \tau+t_{A}^{2}, \quad t^{3}=0, \quad x^{1}=x_{A}^{1} \neq 0, \quad x^{2}=0, \quad x^{3}=0 \tag{26}
\end{equation*}
$$

where $\left(u^{1}\right)^{2}+\left(u^{2}\right)^{2}=1$. For the source world line we keep Eq. (23). Inserting (26) into the light cone equation (24), we have

$$
\begin{equation*}
\left(u^{1} \tau-\tau_{0}\right)^{2}+\left(u^{2} \tau+t_{A}^{2}\right)^{2}-\left(x_{A}^{1}\right)^{2}=0 . \tag{27}
\end{equation*}
$$

From the latter equation we obtain

$$
\begin{equation*}
\tau=-\left(u^{2}-u^{1} \tau_{0}\right) \pm \sqrt{\left(u^{2} t_{A}^{2}-u^{1} \tau_{0}\right)^{2}-\left(\tau_{0}^{2}+\left(t_{A}^{2}\right)^{2}-\left(x_{A}^{1}\right)^{2}\right)} \tag{28}
\end{equation*}
$$

This has a solution, if the discriminant is positive:

$$
\begin{equation*}
\left(u^{2} t_{A}^{2}-u^{1} \tau_{0}\right)^{2}-\left(\tau_{0}^{2}+\left(t_{A}^{2}\right)^{2}-\left(x_{A}^{1}\right)^{2}\right)>0 \tag{29}
\end{equation*}
$$

This holds for a certain interval of the $\tau_{0}$ values that can be found by solving the quadratic equation

$$
\begin{equation*}
-\left(u^{2}\right)^{2} \tau_{0}^{2}-2 u^{1} u^{2} t_{A}^{2} \tau_{0}+\left(t_{A}^{2}\right)^{2}\left(\left(u^{2}\right)^{2}-1\right)+\left(x_{A}^{1}\right)^{2}=0 \tag{30}
\end{equation*}
$$

which gives

$$
\begin{equation*}
\tau_{0}=\frac{-u^{1} t_{A}^{2} \mp x_{A}^{1}}{u^{2}} . \tag{31}
\end{equation*}
$$

Assuming $x_{A}^{1}>0$, the source $B$ is visible for the observer $A$ within the interval

$$
\begin{equation*}
\frac{-u^{1} t_{A}^{2}-x_{A}^{1}}{u^{2}}<\tau_{0}<\frac{-u^{1} t_{A}^{2}+x_{A}^{1}}{u^{2}} \tag{32}
\end{equation*}
$$

Recall that $\tau_{0}=t_{B}^{1}$ is the time of emission. The corresponding time of detection $\tau=\sqrt{\left(t^{1}\right)^{2}+\left(t^{2}\right)^{2}}$ can be calculated from Eq. (28). Since detection of light by the observer $A$ must be after its emission by the source $B$, we require $\tau>\tau_{0}$. The latter requirement determines the sign in Eq. (28). Thus, if $u^{1}>0$, one must take the positive sign in fron of the square root. Outside the interval (32), the source is invisible for $A$.

Dark matter could be an effect of a higher dimensional spacetime with extra time like dimensions. Certain matter, whose worldlines are parallelly displaced in multitime with respect to our worldline, is dark all the time. Those worldlines that are
inclined in multi-time, are visible to us for a certain time period, and invisible before and after that period. For astrophysical objects such period is very long, because the distance from the source, $x_{A}^{1}$, occurring in Eq. (32), is very large. Therefore, it is unlikely that we will suddenly see the appearance of a new object or the disappearance of an existing one. Moreover, since the object consists of many particles whose world lines have different directions in multi-tim\& $\sqrt{4}$, the appearance or disappearance of such object would not be sudden, but gradual. From Eq. (31) we estimate the transition period to be $\Delta \tau_{0} \approx\left(x_{A}^{1} / u^{2}\right)\left(\Delta u^{2} / u^{2}\right)$, where $\Delta u^{2}$ is the average spread of $u^{2}$. Taking, e.g., $x_{A}^{1} \approx 10^{5}$ light years, $u^{2} \approx 10^{-3}$, and $\Delta u^{2} / u^{2} \approx 10^{-5}$, we obtain $\Delta \tau_{0} \approx 10^{3}$ years. Thus, on the Earth, we would just see a faint astrophysical object, and centuries or millennia later the future astronomers will eventually see that those objects have become slightly fainter or slightly more luminous.

## 4 Conclusion

Spaces $M_{n, n}$ with multiple time dimensions admit apparent superluminal motion in the 4-dimensional spacetime $M_{1,4}$. We have investigated whether this could be an explanation for the superluminal neutrinos found in the OPERA experiment. Using the generalized expression for a particle's energy, we have found 5 that a 17 GeV muon neutrino traveling with the speed $v / c=1+2.48 \times 10^{-5}$ has an imaginary effective 4D mass of 120 MeV . The latter mass is an invariant under Lorentz transformations in $M_{1,4}$, but not in $M_{n, n}$, and is the sum of two contributions. One contributions comes from the invariant mass $M$ in $M_{n, n}$, whereas the other contribution comes from the momenta in the extra time like dimensions. The mass $M$ is the true mass of neutrino, and it can be small. Our conclusion is that the OPERA superluminal muon neutrinos can be explained in terms of the relativity in $M_{n, n}$. In this paper we have considered a generic space with time like dimensions. In particular, a candidate for such space is the Clifford space [12].

We also point out, and rederive in a different way, a known result [15, 8] that the special relativity in $M_{n, n}$ predicts dark matter. Such an extended relativity is thus not only able to explain superluminal neutrinos, but also dark matter. If the theory is generalized to curved spaces, then, à la Kaluza-Klein, it can describe other interactions, besides the 4D gravity. This possibility has been explored within the context of Clifford space [17, 18].

A great stumbling block against the acceptance of the possibility of superluminal velocities is the issue of causality. But if the superluminal velocities found in the

[^2]OPERA experiment are confirmed ${ }^{6}$ by other independent experiments, this will pave a way for a reconsideration of the usual causality arguments. In the literature there already exist alternative explanations [7, 10. Causality paradoxes of tachyons can be resolved [7, [10] in the same way as David Deutsch resolved [19] the time travel paradoxes of wormholes: By considering multiverse and the Everett interpretation of quantum mechanics [20]. The existence of superluminal particles, as well as the existence of time travel, is in agreement with the Everett interpretation, but not with the other known interpretations of quantum mechanics.

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[^0]:    ${ }^{1}$ We assume that $\tau=t^{1}$ is the proper time of the observer $\mathcal{O}$ who measures the momentum $p^{a}=\left(\tilde{p}^{1}, \tilde{p}^{2}, \tilde{p}^{3}, p^{1}, p^{2}, p^{3}\right)$ of the particle. A particle that is at rest with respect to $\mathcal{O}$ has then only the first component of momentum different from zero: $p^{\prime a}=\left(\tilde{p}^{1}, 0,0,0,0,0\right)$. Therefore, for the observer $\mathcal{O}$, the $\tilde{p}^{\prime 1}$ and $\tilde{p}^{1}$ are the energies of the particles.

[^1]:    ${ }^{2}$ Here we distinguish the weak eigenstates, $e, \mu, \tau$, from the mass eigenstates, $e^{\prime}, \mu^{\prime}, \tau^{\prime}$, by using prime, though more common notation is $1,2,3$.
    ${ }^{3}$ In Refs. [15] 8], the authors consider the light cones that originate from the observer. Therefore, strictly speaking, they find under which conditions the observer is not seen by the particle. But

[^2]:    ${ }^{4}$ This is a very natural assumption, because the object's worldlines also have different directions in 3 -space, i.e, different velocities (not all particle forming the object move in the same direction and with the same speed).
    ${ }^{5}$ See also an alternative procedure of Ref. [14.

[^3]:    ${ }^{6}$ If the OPERA result turns out to be explicable in more conventional terms, there still remains a possibility that, in the future, superluminal motions will be observed in a different experimental setup.

